Surname	Other na	mes
Pearson Edexcel GCE	Centre Number	Candidate Number
Statistics Advanced/Advan		
Monday 27 June 2016 – Time: 1 hour 30 minut	•	Paper Reference 6684/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Values from the statistical tables should be quoted in full. When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
 use this as a quide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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1. A student is investigating the numbers of cherries in a *Rays* fruit cake. A random sample of *Rays* fruit cakes is taken and the results are shown in the table below.

Number of cherries	0	1	2	3	4	5	≥6
Frequency	24	37	21	12	4	2	0

(a) Calculate the mean and the variance of these data.

(3)

(b) Explain why the results in part (a) suggest that a Poisson distribution may be a suitable model for the number of cherries in a *Rays* fruit cake.

(1)

The number of cherries in a Rays fruit cake follows a Poisson distribution with mean 1.5

A Rays fruit cake is to be selected at random.

Find the probability that it contains

- (c) (i) exactly 2 cherries,
 - (ii) at least 1 cherry.

(4)

Rays fruit cakes are sold in packets of 5

(d) Show that the probability that there are more than 10 cherries, in total, in a randomly selected packet of *Rays* fruit cakes, is 0.1378 correct to 4 decimal places.

(3)

Twelve packets of *Rays* fruit cakes are selected at random.

(e) Find the probability that exactly 3 packets contain more than 10 cherries.

(3)

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Question 1 continued	
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Question 1 continued		Jank
		Q1
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	(Total 14 marks)	



2.	In a region of the UK, 5% of people have red hair. In a random sample of size n , taken from this region, the expected number of people with red hair is 3
	(a) Calculate the value of <i>n</i> . (2)
	A random sample of 20 people is taken from this region. Find the probability that
	(b) (i) exactly 4 of these people have red hair,
	(ii) at least 4 of these people have red hair. (5)
	Patrick claims that <i>Reddman</i> people have a probability greater than 5% of having red hair. In a random sample of 50 <i>Reddman</i> people, 4 of them have red hair.
	(c) Stating your hypotheses clearly, test Patrick's claim. Use a 1% level of significance. (5)

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	Q2
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3.	The random variable R has a continuous uniform distribution over the interval $[5, 9]$	
	(a) Specify fully the probability density function of R .	(1)
		(1)
	(b) Find $P(7 < R < 10)$	(1)
	The mandam vanishle dig the area of a simple modive Dom	()
	The random variable A is the area of a circle radius R cm.	
	(c) Find $E(A)$	(4)
		(•)

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A continuous random variable X has cumulative distribution function F(x) given by

$$F(x) = \begin{cases} 0 & x < 2 \\ k(ax + bx^2 - x^3) & 2 \le x \le 3 \\ 1 & x > 3 \end{cases}$$

Given that the mode of X is $\frac{8}{3}$

(a) show that b = 8

(6)

(b) find the value of k.

(4)

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Question 4 continued	



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	Q4
(Total 10 marks)	



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n stud	arge school, 20% of students own a touch screen laptop. A random sample of dents is chosen from the school. Using a normal approximation, the probability more than 55 of these n students own a touch screen laptop is 0.0401 correct to difficant figures.
Find 1	the value of n . (8)
	(6)

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6. A bag contains a large number of counters with one of the numbers 4, 6 or 8 written on each of them in the ratio 5:3:2 respectively.

A random sample of 2 counters is taken from the bag.

(a) List all the possible samples of size 2 that can be taken.

(2)

The random variable *M* represents the mean value of the 2 counters.

Given that $P(M = 4) = \frac{1}{4}$ and $P(M = 8) = \frac{1}{25}$

(b) find the sampling distribution for M.

(5)

A sample of n sets of 2 counters is taken. The random variable Y represents the number of these n sets that have a mean of 8

(c) Calculate the minimum value of *n* such that $P(Y \ge 1) > 0.9$

(3)



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7. The weight, $X \log$, of staples in a bin full of paper has probability density function

$$f(x) = \begin{cases} \frac{9x - 3x^2}{10} & 0 \le x < 2\\ 0 & \text{otherwise} \end{cases}$$

Use integration to find

(a) E(X)

(4)

(b) Var (*X*)

(4)

(c) P(X > 1.5)

(3)

Peter raises money by collecting paper and selling it for recycling. A bin full of paper is sold for £50 but if the weight of the staples exceeds 1.5 kg it sells for £25

(d) Find the expected amount of money Peter raises per bin full of paper.

(2)

Peter could remove all the staples before the paper is sold but the time taken to remove the staples means that Peter will have 20% fewer bins full of paper to sell.

(e) Decide whether or not Peter should remove all the staples before selling the bins full of paper. Give a reason for your answer.

(2)



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